



# Tangents to a Circle

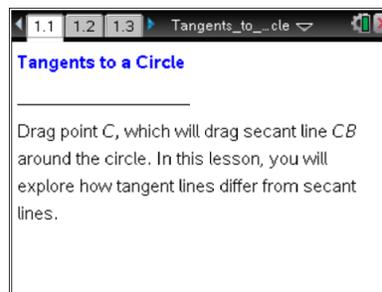
## Student Activity

Name \_\_\_\_\_

Class \_\_\_\_\_

Open the TI-Nspire document *Tangents\_to\_a\_Circle.tns*.

A line that intersects a circle in two points is called a secant. What is a tangent line, and how does it differ from a secant line? This activity will explore properties of tangents.



Move to page 1.2.

Press **ctrl** **▶** and **ctrl** **◀** to navigate through the lesson.

$\overline{CP}$  is a secant of circle  $A$ .  $\angle CBA$  has been measured. Dragging point  $C$  also drags the  $\overline{CP}$  around the circle. As you drag  $C$ , points  $P$  and  $B$  will move away from each other or closer to each other.

1. a. As you drag point  $C$ , what happens to  $\angle CBA$ ?
  
  
  
  
  
  
  
  
  
  
- b. When points  $P$  and  $B$  are very close to each other, what is the measure of  $\angle CBA$ ? What happened to point  $P$ ?
  
  
  
  
  
  
  
  
  
  
- c. When  $\angle CBA$  measures  $0^\circ$ , where is point  $P$  on the circle in relation to  $B$ ?
  
  
  
  
  
  
  
  
  
  
- d. When  $\angle CBA$  measures  $90^\circ$ , what has happened to the secant line?

Move to page 1.3.

A tangent line has been constructed at point  $T$ . Drag point  $B$  to move the tangent line around the circle.

2. A tangent line intersects the circle in exactly one point, which is known as the point of tangency. How is a tangent related to the radius at the point of tangency?



**Move to page 2.1.**

This page shows two tangent lines intersecting at point  $B$ .

3. Drag point  $B$  and observe the tangent segments  $\overline{AB}$  and  $\overline{BC}$ .
  - a. What can you conjecture about the tangent segments  $\overline{AB}$  and  $\overline{BC}$ ?
  
  
  
  
  
  
  
  
  
  
  - b. What happens to the tangent segments when  $B$  is inside the circle? Why?
  
  
  
  
  
  
  
  
  
  
  - c. Click  $\Delta$  to show the radii and  $\overline{OB}$ . Look at the triangles formed from the segments. What do you notice about  $\triangle AOB$  and  $\triangle COB$ ?

**Move to page 3.1.**

4. Prove that  $\overline{AB} \cong \overline{CB}$ .
  - a. Click  $\Delta$  to draw  $\overline{OA}$  and  $\overline{OC}$ . Click  $\Delta$  to show the next step. Why is  $\overline{OA} \cong \overline{OC}$ ?
  
  
  
  
  
  
  
  
  
  
  - b. Click  $\Delta$  to show the next step. Why is  $\overline{OA} \perp \overline{AB}$ ? Why is  $\overline{OC} \perp \overline{CB}$ ?
  
  
  
  
  
  
  
  
  
  
  - c. Click  $\Delta$  to show the next steps. Why is  $\triangle AOB \cong \triangle COB$ ?
  
  
  
  
  
  
  
  
  
  
  - d. Why can you conclude  $\overline{AB} \cong \overline{CB}$ ?